Dielectron azimuthal anisotropy at mid-rapidity in Au + Au collisions at \( \sqrt{s_{NN}} = 200 \) GeV


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We report on the first measurement of the azimuthal anisotropy ($v_2$) of dielectrons ($e^+e^-$ pairs) at mid-rapidity from $\sqrt{s_{NN}} = 200$ GeV Au + Au collisions with the STAR detector at the Relativistic Heavy Ion Collider (RHIC), presented as a function of transverse momentum ($p_T$) for different invariant-mass regions. In the mass region $M_{ee} < 1.1$ GeV/c$^2$, the dielectron $v_2$ measurements are found to be consistent with expectations from $\pi^0$, $\eta$, $\omega$, and $\phi$ decay contributions. In the mass region $1.1 < M_{ee} < 2.9$ GeV/c$^2$, the measured dielectron $v_2$ is consistent, within experimental uncertainties, with that from the $c\bar{c}$ contributions.

DOI: 10.1103/PhysRevC.90.064904 PACS number(s): 25.75.Cj, 25.75.Ld

I. INTRODUCTION

Dileptons are among the most essential tools for investigating the strongly interacting matter created in ultrarelativistic heavy-ion collisions [1,2]. Once produced, leptons, like photons, are not affected by the strong interaction. Unlike photons, however, dileptons have an additional kinematic dimension: their invariant mass. Different kinematics of lepton pairs [mass and transverse momentum ($p_T$) ranges] can selectively probe...
the properties of the created matter throughout the whole evolution [3,4].

In the low invariant mass range of produced lepton pairs ($M_{ll} < 1.1\text{ GeV}/c^2$), vector mesons such as $\rho(770)$, $\omega(782)$, and $\phi(1020)$ and Dalitz decays of pseudoscalar mesons ($\pi^0$ and $\eta$) dominate the spectrum. In-medium properties of the spectral functions of these vector mesons may exhibit modifications related to possible chiral symmetry restoration [3,4], which can be studied via their dilepton decays. At the Super Proton Synchrotron (SPS), the low-mass dilepton enhancement in the CERES $e^+e^-$ data [5] and in the NA60 $\mu^+\mu^-$ data [6] could be attributed to substantial medium modification of the $\rho$-meson spectral function. Two different realizations of chiral symmetry restoration were proposed: a dropping-mass scenario [7] and a broadening of the $\rho$ spectral function [8], both of which described the CERES data. The precise NA60 measurement has provided a decisive discrimination between the two scenarios, with only the broadened spectral function [9] being able to describe the data.

At the Relativistic Heavy Ion Collider (RHIC), a significant enhancement in the dilepton continuum, compared to expectations from hadronic sources for $0.15 < M_{ee} < 0.75\text{ GeV}/c^2$, was observed by the PHENIX Collaboration in Au + Au collisions at $\sqrt{s_{NN}} = 200\text{ GeV}$ [10]. This enhancement is reported to increase from peripheral to central Au + Au collisions and has a strong $p_T$ dependence. At low $p_T$ (below 1 GeV/c), the enhancement factor increases from $1.5 \pm 0.5_{\text{stat}} \pm 0.5_{\text{syst}} \pm 0.3_{\text{model}}$ in 60–92% peripheral Au + Au collisions to $7.6 \pm 0.5_{\text{stat}} \pm 1.3_{\text{syst}} \pm 1.5_{\text{model}}$ in 0–10% central Au + Au collisions. The last error is an estimate of the uncertainty in the extracted yield due to known hadronic sources. The STAR Collaboration recently reported dilepton spectra in Au + Au collisions at $\sqrt{s_{NN}} = 200\text{ GeV}$, demonstrating an enhancement with respect to the contributions from known hadronic sources in the low-mass region that bears little centrality dependence [11]. Theoretical calculations [12–14], which describe the SPS dilepton data, fail to consistently describe the low-$p_T$ and low-mass enhancement observed by PHENIX in 0–10% and 10–20% central Au + Au collisions [10]. The same calculations, however, describe the STAR measurement of the low-$p_T$ and low-mass enhancement from peripheral to central Au + Au collisions [11].

For $1 < p_T < 5\text{ GeV}/c$ and in the mass region $M_{ee} < 0.3\text{ GeV}/c^2$, the PHENIX Collaboration derived direct photon yields through dielectron measurements to assess thermal radiation at RHIC [15]. The excess of direct photon yield in central Au + Au collisions over that observed in $p + p$ collisions is found to fall off exponentially with $p_T$ with an inverse slope of $220\text{ MeV}$. In addition, the azimuthal anisotropy $v_2$, the second harmonic of the azimuthal distribution with respect to the event plane [16], has been measured for direct photons using an electromagnetic calorimeter and found to be substantial and comparable to the $v_2$ for hadrons for $1 < p_T < 4\text{ GeV}/c$ [17]. Model calculations for thermal photons from the quark-gluon plasma (QGP) in this kinematic region significantly underpredict the observed $v_2$, while the model calculations which include a significant contribution from the hadronic sources at a later stage describe the excess of the spectra and the substantial $v_2$ for $1 < p_T < 4\text{ GeV}/c$ reasonably well [18]. With their augmented kinematics, dilepton $v_2$ measurements have been proposed as an alternative study of medium properties [19]. Specifically, the $v_2$ as a function of $p_T$ in different invariant mass regions will enable us to probe the properties of the medium at different stages, from QGP to hadron-gas dominated.

The dilepton spectra in the intermediate mass range ($1.1 < M_{ll} < 3.0\text{ GeV}/c^2$) are expected to be related to the QGP thermal radiation [3,4]. However, contributions from other sources have to be measured experimentally, e.g., electron or muon pairs from semileptonic decays of open charm or broad hadrons ($c \rightarrow l^+l^- X$ or $b \rightarrow l^+l^- X$). Utilizing dielectrons, the PHENIX Collaboration obtained the charm and bottom cross sections in $p+p$ collisions at $\sqrt{s} = 200\text{ GeV}$ [20].

With the installation of a time-of-flight (TOF) detector [21], as well as an upgrade of the data acquisition system [22], the STAR detector with its large acceptance provides excellent electron identification capability at low momentum for dielectron analyses [23].

In this paper, we present the first dielectron $v_2$ measurements from low to intermediate mass ($M_{ll} < 2.9\text{ GeV}/c^2$) in Au + Au collisions at $\sqrt{s_{NN}} = 200\text{ GeV}$. This paper is organized as follows. Section II describes the detector and data samples used in the analysis. Sections III A and III B describe the electron identification, electron pair distributions, and background subtraction. Sections III C and III D describe the analysis details of the azimuthal anisotropy and simulation. Section IV describes the systematic uncertainties. Results for the centrality, mass, and $p_T$ dependence of dielectron $v_2$ are presented in detail in Sec. V. Lastly, Sec. VI provides a concluding summary.

II. DETECTOR AND DATA SAMPLE

The two main detectors used in this analysis are the Time Projection Chamber (TPC) [24] and the TOF detector. Both have full azimuthal coverage at mid-rapidity. The TPC is STAR’s main tracking detector, measuring momentum, charge, and energy loss of charged particles. The ionization energy loss ($dE/dx$) of charged particles in the TPC gas is used for particle identification [25,26]. In addition, the TOF detector extends STAR’s hadron identification capabilities to higher momenta and significantly improves its electron identification capabilities [27,28].

The data used for this analysis were taken in 2010 and 2011. A total of 760 million minimum-bias events, with 240 million from 2010 and 520 million from 2011 data samples of $\sqrt{s_{NN}} = 200\text{ GeV}$. Au + Au collisions were used in the analysis. These events were required to have collision vertices within 30 cm of the TPC center along the beam line, where the material budget is minimal (0.6% in radiation length in front of the TPC inner field cage). The minimum-bias trigger was defined by the coincidence of signals from the two Vertex Position Detectors (VPDs) [29], located on each side of the STAR barrel, covering a pseudorapidity range of 4.4 < $|\eta|$ < 4.9. The centrality tagging was determined by the measured charged particle multiplicity density in the TPC within $|\eta| < 0.5$ [30]. The 2010 and 2011 minimum-bias data (0–80% centrality) were
TABLE I. Criteria used for the selection of tracks for electron identification. NFit is the number of points used to fit the TPC track, and NMax is the maximum possible number for that track. $dE/dx$ points is the number of points used to derive the $dE/dx$ value. The DCA is the distance of the closest approach between the trajectory of a particle and the collision vertex.

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analyzed separately. The dielectron $v_2$ measurement in this article is the combined $v_2$ result from these two data sets.

III. DATA ANALYSIS

A. Electron identification

Particles directly originating from the collision, with trajectories that project back to within 1 cm of the collision vertex, calculated in three dimensions, were selected for this analysis. Table I lists selection criteria for the tracks for further electron identification. The normalized $dE/dx$ ($n_\sigma e$) is defined as $n_\sigma e = \ln(dE/dx/I_e)/R_e$, where $dE/dx$ is the measured energy loss of a particle, and $I_e$ is the expected $dE/dx$ of an electron. $R_e$ is the resolution of $\ln(dE/dx/I_e)$, defined as the width of its distribution, and is better than 8% for these data. Figure 1(a) shows the $n_\sigma e$ distribution as a function of momentum from the TPC, while panel (b) shows the inverse velocity $1/\beta$ measurements from the TOF versus the momentum measured by the TPC. Panel (c) shows the $n_\sigma e$ distribution versus momentum with the requirement on velocity that $|1/\beta - 1/\beta_{\exp}| < 0.025$, in which $\beta_{\exp}$ is the velocity calculated with the assumption of electron mass. Panel (d) presents the $n_\sigma e$ distribution for $0.68 < p_T < 0.73$ GeV/c after the cut $|1/\beta - 1/\beta_{\exp}| < 0.025$ is applied. With perfect calibration, the $n_\sigma e$ for single electrons should follow a standard normal distribution. Electron candidates whose $n_\sigma e$ falls between the lines in Fig. 1(c) are selected. From the multiple-component fit to the $dE/dx$ distribution, an example of which is shown in panel (d), one can obtain the purity of electron candidates. The purity is 95% on average and depends on momentum [11], as shown in Fig. 2. With the combined information of velocity ($\beta$) from the TOF and $dE/dx$ from the TPC, electrons can be clearly identified from low to intermediate $p_T$ (0.2 < $p_T$ < 3 GeV/c) for $|\eta| < 1$ [31,32]. This is important for dielectron measurements from the low to intermediate mass region.

![Figure 1](image-url)
Unlike-sign (mixed)

would also be contained in the data. Radiation and additional contributions from the hadron gas include flavor and heavy-flavor hadrons. The light-flavor sources in the shading around the data points.

The dielectron + function of momentum in minimum-bias Au + Au include flavor and heavy-flavor hadrons. The light-flavor sources in the shading around the data points. Results in large uncertainties in the multi-component fit, as shown by the shading around the data points.

B. Dielectron invariant mass distribution and background subtraction

The dielectron signals may come from decays of both light-flavor and heavy-flavor hadrons. The light-flavor sources include η, η', and η' Dalitz decays: π⁰ → γe⁺e⁻, η → γe⁺e⁻, and η' → γe⁺e⁻e⁻; and vector meson decays: ω → π⁰e⁺e⁻, ω → e⁺e⁻, ρ⁰ → e⁺e⁻, φ → ηe⁺e⁻, and φ → e⁺e⁻. The heavy-flavor sources include J/ψ → e⁺e⁻ and heavy-flavor hadron semileptonic decays: c ¯c → e⁺e⁻ and bb → e⁺e⁻e⁻. The signals also include Drell-Yan contributions. The dielectron contributions from photon conversions (γ → e⁺e⁻) in the detector material are present in the raw data. The momenta of these electrons are biased, which results in a multiple-peak structure in the dielectron mass distribution for Mₑₑ < 0.12 GeV/c². The peak position in the mass distribution depends on the conversion point in the detector [33]. It is found that the dielectron v2 from photon conversions is the same as that from π⁰ Dalitz decays. The vector meson contributions to the Au + Au data may be modified in the medium. QGP thermal radiation and additional contributions from the hadron gas would also be contained in the data.

With high-purity electron samples, the e⁺e⁻ pairs from each event are accumulated to generate the invariant mass distributions (Mₑₑ), here referred to as the unlike-sign distributions. The unlike-sign distributions contain both signal (defined in the previous paragraph) and backgrounds of random combinatorial pairs and correlated cross pairs. The correlated cross pairs come from two e⁺e⁻ pairs from a single meson decay: a Dalitz decay followed by a conversion of the decay photon, or conversions of multiple photons from the same meson. The electron candidates are required to be in the range |η| < 1 and pT > 0.2 GeV/c, while the rapidity of e⁺e⁻ pairs (ηₑₑ) is required to be in the region |yₑₑ| < 1.

Two methods are used for background estimation, based on same-event like-sign and mixed-event unlike-sign techniques. In the mixed-event technique, tracks from different events are used to form unlike-sign or like-sign pairs. The events are divided into 9000 categories according to the collision vertex (10 bins), event plane (defined in Sec. III C) azimuthal angle (100 bins from 0 to π/2), and centrality (9 bins). The two events to be mixed must come from the same event category to ensure similar detector geometric acceptance, azimuthal anisotropy, and track multiplicities. We find that when the number of event plane bins is larger than or equal to 30, the mixed-event spectrum describes the combinatorial background.

In the same-event like-sign technique, electrons with the same charge sign from the same events are paired. Due to the sector structure of the TPC, and the different bending directions of positively and negatively charged particle tracks in the transverse plane, like-sign and unlike-sign pairs have different acceptances. The correction for this acceptance difference is applied to the same-event like-sign pair distribution before background subtraction. The acceptance difference between same-event unlike-sign and same-event like-sign pairs is obtained using the mixed-event technique. Figure 3(a) shows the mixed-event unlike-sign and mixed-event like-sign electron pair invariant mass distributions in √sNN = 200 GeV minimum-bias Au + Au collisions. The ratio of these two distributions, the acceptance difference factor, is shown in Fig. 3(b), and its zoom-in version is shown in Fig. 3(c). The centrality and pT dependences are presented in Figs. 4 and 5, respectively. These figures show that the acceptance...
FIG. 4. (Color online) The ratio of the mixed-event like-sign distribution to the mixed-event unlike-sign distribution in minimum-bias Au + Au collisions at $\sqrt{s_{NN}} = 200$ GeV, as well as specific centrality selections of the collisions.

FIG. 5. (Color online) The ratio of the mixed-event like-sign distribution to the mixed-event unlike-sign distribution in different $p_T$ ranges in minimum-bias Au + Au collisions at $\sqrt{s_{NN}} = 200$ GeV.

FIG. 6. (a) The electron pair invariant mass distributions for same-event unlike-sign pairs, same-event like-sign pairs, and mixed-event unlike-sign pairs in minimum-bias Au + Au collisions at $\sqrt{s_{NN}} = 200$ GeV. The electron candidates are required to be in the range $|\eta| < 1$ and have $p_T$ greater than 0.2 GeV/c. The $ee$ pairs are required to be in the rapidity range $|y_{ee}| < 1$. Variable bin widths are used for the yields and signal-to-background ratios. (b) The ratio of the same-event like-sign distribution (corrected for the acceptance difference) to the normalized mixed-event unlike-sign distribution in minimum-bias Au + Au collisions at $\sqrt{s_{NN}} = 200$ GeV. (c) A zoom-in version of panel (b).

After correcting for the acceptance difference, the same-event like-sign distribution is compared to the same-event unlike-sign pair distribution (which contains the signal) and the mixed-event unlike-sign pair distribution in Fig. 6(a). The mixed-event unlike-sign distribution is normalized to match the same-event like-sign distribution in the mass region 0.9–3.0 GeV/c$^2$. For $M_{ee} > 0.9$ GeV/c$^2$, the ratio of the same-event like-sign distribution over the normalized mixed-event unlike-sign distribution is found constant with $\chi^2$/NDF of 15/16, as shown in Fig. 6(b). The constant is $0.9999 \pm 0.0004$. The zoom-in version, centrality dependence, and $p_T$ dependence of this ratio are shown in Figs. 6(c), 7, and 8, respectively. In addition, the centrality and $p_T$ dependences of the ratio of the same-event like-sign distribution over the normalized mixed-event like-sign distribution are presented in Figs. 9 and 10, respectively.

In the low-mass region, the correlated cross-pair background is present in the same-event like-sign distribution, but not in the mixed-event unlike-sign background. In the higher mass region, the mixed-event unlike-sign distribution

...
FIG. 7. (Color online) The centrality dependence of the ratio of the same-event like-sign distribution (corrected for the acceptance difference) to the normalized mixed-event unlike-sign distribution in minimum-bias Au + Au collisions at $\sqrt{s_{NN}} = 200$ GeV.

FIG. 9. (Color online) The centrality dependence of the ratio of the same-event like-sign distribution to the normalized mixed-event like-sign distribution in minimum-bias Au + Au collisions at $\sqrt{s_{NN}} = 200$ GeV.

FIG. 8. (Color online) The $p_T$ dependence of the ratio of the same-event like-sign distribution (corrected for the acceptance difference) to the normalized mixed-event unlike-sign distribution in minimum-bias Au + Au collisions at $\sqrt{s_{NN}} = 200$ GeV.

FIG. 10. (Color online) The $p_T$ dependence of the ratio of the same-event like-sign distribution to the normalized mixed-event like-sign distribution in minimum-bias Au + Au collisions at $\sqrt{s_{NN}} = 200$ GeV.
matches the same-event like-sign distribution. Therefore, for $M_{ee} < 0.9 \text{ GeV}/c^2$ like-sign pairs from the same events are used for background subtraction. For $M_{ee} > 0.9 \text{ GeV}/c^2$ we subtract the mixed-event unlike-sign background to achieve better statistical precision.

Figure 11 shows the $p_T$ as a function of $M_{ee}$ for the dielectron continuum after background subtraction without efficiency correction in $\sqrt{s_{NN}} = 200 \text{ GeV}$ minimum-bias Au + Au collisions.

![Figure 11](image)

**FIG. 11.** (Color online) The $p_T$ as a function of $M_{ee}$ for dielectron signal without efficiency correction in $\sqrt{s_{NN}} = 200 \text{ GeV}$ minimum-bias Au + Au collisions. The two-peak structure, as shown in the inset, for $M_{ee} < 0.12 \text{ GeV}/c^2$ is due to photon conversions in the beam pipe and supporting structure. Errors are statistical only. (b) The signal-over-background ratio in $\sqrt{s_{NN}} = 200 \text{ GeV}$ minimum-bias Au + Au collisions. The first two data points are not shown for clarity. Errors are statistical.

C. Method to obtain azimuthal anisotropy

Hydrodynamic flow of produced particles leads to azimuthal correlations among particles relative to the reaction plane [16]. However, the measured correlations also include effects not related to reaction plane orientation. These are usually referred to as nonflow, and are due to, for example, resonance decays and parton fragmentation. In this analysis, we use the “event-plane” method to determine the azimuthal anisotropy of produced dielectrons [16].

The event plane is reconstructed using tracks from the TPC. The event flow vector $Q_2$ and the event-plane angle $\Psi_2$ are defined by [16]

\[
Q_2 \cos(2\Psi_2) = Q_{2x} = \sum_i w_i \cos(2\phi_i), \quad (1)
\]

\[
Q_2 \sin(2\Psi_2) = Q_{2y} = \sum_i w_i \sin(2\phi_i), \quad (2)
\]

\[
\Psi_2 = \left( \frac{\tan^{-1} \frac{Q_{2x}}{Q_{2y}}}{2} \right), \quad (3)
\]

where the summation is over all particles $i$ used for event-plane determination. Here, $\phi_i$ and $w_i$ are measured azimuthal angle and weight for the particle $i$, respectively. The weight $w_i$ is equal to the particle $p_T$ up to 2 GeV/c, and is kept constant at higher $p_T$. The electron candidates are excluded in the event-plane reconstruction to avoid the self-correlation effect. A PYTHIA study indicates that decay kaons from heavy flavor have no additional effect on event-plane determination.

An azimuthally nonhomogeneous acceptance or efficiency of the detectors can introduce a bias in the event-plane reconstruction which would result in a nonuniform $\Psi_2$ angle distribution in the laboratory coordinate system. The recentering and shifting methods [34,35] were used to flatten the $\Psi_2$ distribution.

The observed $v_2$ is the second harmonic of the azimuthal distribution of particles with respect to the event plane:

\[
v_2^{\text{obs}} = \langle \cos(2(\phi - \Psi_2)) \rangle, \quad (4)
\]

where angle brackets denote an average over all particles with azimuthal angle $\phi$ in a given phase space and $\phi - \Psi_2$ ranges from 0 to $\pi/2$. The electron reconstruction efficiency is independent of $\phi - \Psi_2$. The real $v_2$ is corrected for event-plane resolution as

\[
v_2 = \frac{v_2^{\text{obs}}}{C \sqrt{\left( \cos \left[ 2(\Psi_2^y - \Psi_2^z) \right] \right)}, \quad (5)
\]

where $\Psi_2^y$ and $\Psi_2^z$ are the second-order event planes determined from different subevents, $C$ is a constant calculated from the known multiplicity dependence of the resolution [16], and the
The event-plane resolution for different centralities in 200 GeV Au collisions at $\sqrt{s_{NN}} = 200$ GeV.

brackets denote an average over a large event sample. The denominator represents the event-plane resolution, which is obtained from two random subevents [36]. Figure 13 shows the event-plane resolution for different centralities in 200 GeV Au + Au collisions.

The $v_2$ for dielectron signals for each mass and $p_T$ bin is obtained using the formula

$$v_2^S(M_{ee}, p_T) = \frac{v_2^{\text{total}}(M_{ee}, p_T)}{r(M_{ee}, p_T)} - \frac{1 - r(M_{ee}, p_T)}{r(M_{ee}, p_T)} v_2^B(M_{ee}, p_T),$$

in which $v_2^S$, $v_2^{\text{total}}$, and $v_2^B$ represent $v_2$ for the dielectron signal, $v_2$ for the same-event unlike-sign electron pairs, and $v_2$ for the background electron pairs (determined through either the mixed-event unlike-sign technique or the same-event like-sign method, as discussed in the previous sections), respectively. The parameter $r$ represents the ratio of the number of dielectron signals ($N_S$) to the number of the same-event unlike-sign electron pairs ($N_{S+B}$). The $v_2^{\text{total}}$ is the yield-weighted average from the dielectron signal and background. The mixed-event

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FIG. 13. The event-plane resolution from central to peripheral (left to right) collisions in minimum-bias Au + Au collisions at $\sqrt{s_{NN}} = 200$ GeV.

unlike-sign technique is applied for $M_{ee} > 0.9$ GeV/c$^2$, for which the mixed-event unlike-sign distribution for each of the $(\phi - \Psi_2)$ bins (the bin width is $\frac{\pi}{10}$) is normalized to the corresponding same-event like-sign distribution in the same $\phi - \Psi_2$ bin. For the five $(\phi - \Psi_2)$ bins, the normalization factors differ by 0.1%. Figure 14 shows $v_2^{\text{total}}$ and $v_2^B$ as a function of $M_{ee}$ within the STAR acceptance in minimum-bias Au + Au collisions at $\sqrt{s_{NN}} = 200$ GeV.

D. Cocktail simulation

In the following we wish to obtain a representation of the dielectron $v_2$ distributions in $p_T$ and $M_{ee}$ by a cocktail simulation that accounts for the decays of all prominent hadronic sources. We shall obtain the dielectron $v_2$ from each decay component by combining the measured $p_T$ spectra of the "mother mesons," with the previously measured $v_2$ distributions of these mesons.

As mentioned earlier, the dielectron pairs may come from decays of light-flavor and heavy-flavor hadrons. Contributions from the following hadronic sources and processes were included in the cocktail simulation to compare with the measured data: $\pi^0 \rightarrow \gamma e^+e^-$, $\eta \rightarrow \gamma e^+e^-$, $\omega \rightarrow \pi^0 e^+e^-$, $\omega \rightarrow e^+e^-$, $\phi \rightarrow \eta e^+e^-$, and $\phi \rightarrow e^+e^-$ for $M_{ee} < 1.1$ GeV/c$^2$. In the intermediate mass region, we simulate the dielectron $v_2$ from the $c\bar{c}$ correlated contribution.

The $\pi^0$ invariant yield is taken as the average of $\pi^+$ and $\pi^-$ [37,38]. The $\phi$ yield is taken from STAR measurements [39], while the $\eta$ yield is from a PHENIX measurement [40]. We fit the meson invariant yields with Tsallis functions [41], as shown in Fig. 15(a). The $p_T$-spectrum shape is derived from the Tsallis function. The $\omega$ total yield at mid-rapidity ($dN/dy|_{y=0}$) is obtained by matching the simulated cocktail to the efficiency-corrected dielectron mass spectrum in the $\omega$ peak region. Table II lists the $dN/dy|_{y=0}$ of hadrons in 200 GeV minimum-bias Au + Au collisions. In addition, we parametrize the $\pi$, $K_S^0$, and $\phi v_2$ from previous measurements [36, 42–44] with a data-driven functional form, $A \tanh(B(p_T) + C\arctan(Dp_T)) + E e^{-Fp_T} + F e^{-Gp_T}$, where $A, B, C, D, E,$ and $F$ are fit parameters. The $\eta$ and $\omega$ $v_2$ are assumed to be the same as $K_S^0$ and $\phi$ $v_2$, respectively, since the masses of the $\eta$ and $K_S^0$ mesons, as well as those of the $\omega$ and $\phi$ mesons, are similar. The mass-dependent hydrodynamic behavior was observed for hadron $v_2$ at $p_T < 2$ GeV/c while in the range of $2 < p_T < 6$ GeV/c, the number of constituent quark scaling was observed in Au + Au collisions at $\sqrt{s_{NN}} = 200$ GeV [1,2]. Due to different methods and detector configurations, the nonflow effects vary from 3–5% for charged and neutral $\pi$ measured by PHENIX to 15–20% for charged $\pi$, $K_S^0$, and $\phi$ measured by STAR. Figures 15(b)–15(d) show the previously measured $v_2$ and the fit functions.

With the Tsallis functions for the spectra and the parametrizations for $v_2$ as input, we simulate decays of $\pi^0$, $\eta$, $\omega$, and $\phi$ with appropriate branching ratios (BRs), and obtain the dielectron $v_2$, as shown in Fig. 16. The final $v_2$ is the yield-weighted average from different contributions. The same acceptance conditions after momentum resolution smearing are utilized as those used in the analysis of real
mesons, fit with a function for $\sqrt{s_{NN}} = 200$ GeV, including the contributions from specific decays. The contribution from $\phi \rightarrow \eta e^+e^-$ is smaller than 1% and is not shown for clarity. The bin width is 20 MeV/c$^2$.

In different mass regions different particle species dominate the production, as listed in Table III [11,32]. Studying $v_2$ in different mass regions should therefore help discern the azimuthal anisotropy of different species. Figure 16 shows that among $\pi^0$, $\eta$, $\omega$, and $\phi$ decays, $\pi^0 \rightarrow \gamma e^+e^-$, $\eta \rightarrow \gamma e^+e^-$, $\omega \rightarrow \pi^0 e^+e^-$, $\omega \rightarrow e^+e^-$, and $\phi \rightarrow e^+e^-$ dominate the $v_2$ contribution in the mass regions $[0,0.14]$, $[0.14,0.30]$, $[0.30,0.5]$, $[0.5,0.7]$, $[0.76,0.80]$, and $[0.98,1.06]$ GeV/c$^2$ respectively.

For $1 < M_{ee} < 2.9$ GeV/c$^2$, we simulate the dielectron $v_2$ from $c\bar{c}$ correlated contributions. To get a handle on the unknown $c\bar{c} \rightarrow e^+e^-X$ correlation in Au+Au collisions, we take two extreme approaches to simulate this $v_2$ contribution: (1) we assume the $c$ and $\bar{c}$ are completely uncorrelated; (2) we assume the $c$ and $\bar{c}$ correlation is the same as shown in PYTHIA 6.416, in which the $k_T$ factor is set by PARP(91) = 1 GeV/c, and the parton shower is set by PARP(67) = 1 [47]. With these parameter values, PYTHIA can describe the shape of the $D^0$ [48] spectrum and the nonphotonic electron spectrum measured by STAR [31,49] for $p + p$ collisions.

In Fig. 17, the measured spectrum and $v_2$ of electrons from heavy-flavor decays [50] are shown as well as results of a parametrization which is used to obtain the dielectron $v_2$ from the $c\bar{c}$ contribution. We find that the dielectron $v_2$ from $c\bar{c}$ contribution does not show a significant difference for the two cases explained above. The $v_2$ value is 0.022 for the...
Au collisions at \( \sqrt{s_{NN}} = 200 \text{ GeV} \). The spectrum is fit with a function \( A[e^{B\sqrt{p_{T}^{2}+D(p_{T}^{2}+E)}+\sqrt{p_{T}^{2}+C/E}^2} \), where \( A, B, C, D, E, \) and \( F \) are fit parameters. The \( v_2 \) is fit with the same function as used to parametrize the meson \( v_2 \) shown in Fig. 15.

PYTHIA-correlation case and 0.027 for the uncorrelated case. Therefore, in the subsequent sections, we use the uncorrelated result to compare with our measurements. Figure 18 shows the dielectron \( v_2 \) from the \( c \bar{c} \) contribution as a function of \( M_{\ell\ell} \) and \( p_{T} \) with a completely uncorrelated \( c \) and \( \bar{c} \).

IV. SYSTEMATIC UNCERTAINTIES

The systematic uncertainties for the dielectron \( v_2 \) are dominated by background subtraction. The combinatorial background effect is evaluated by changing the DCA cut of the electron candidates. We vary the DCA cut from less than 1 cm to less than 0.8 cm so that the number of dielectron pairs changes by 20%.

The uncertainties in the correction of the acceptance difference between same-event unlike-sign and same-event like-sign pairs are studied and found to have a negligible contribution.

For \( 0.9 < M_{\ell\ell} < 2.9 \text{ GeV}/c^2 \), there are additional systematic uncertainties from the mixed-event normalization and background subtraction methods. The uncertainty on the mixed-event normalization is obtained by taking the full difference between the results from varying the normalization range from \( 0.9 < M_{\ell\ell} < 3.0 \) to \( 0.7 < M_{\ell\ell} < 3.0 \text{ GeV}/c^2 \). In addition, there can be correlated sources in the same-event like-sign pairs for which the mixed-event background cannot completely account. This would lead to a larger \( v_2 \) for the dielectron signal when using mixed-event background subtraction. Therefore, the full difference between mixed-event unlike-sign and same-event like-sign background subtraction contributes to the lower bound of the systematic uncertainties. In the mass region 0.98–1.06 GeV/c², the full difference between mixed-event unlike-sign and same-event like-sign background subtraction is negligible and not shown in Table IV.

We also evaluate the hadron contamination effect by changing the no\( \sigma_e \) cut. The hadron contamination is varied from 5% to 4% and to 6%. The \( v_2 \) difference between the default value and the new value is quoted as part of the systematic uncertainties, as shown in Table IV.

In addition, we use the \( \eta \)-subevent method [36] to study the systematic uncertainties for the dielectron \( v_2 \) in the \( \pi^0 \) Dalitz decay mass region. An \( \eta \) gap of \( |\eta| < 0.3 \) between positive and negative pseudorapidity subevents is introduced to reduce nonflow effects [36]. The \( v_2 \) difference between the \( \eta \)-subevent method and the default method contributes \((0.1–7.3) \times 10^{-3}\) absolute systematic uncertainties for \( M_{\ell\ell} < 0.14 \text{ GeV}/c^2 \). We do not study this effect for the dielectron \( v_2 \) in the other mass regions due to limited statistics. However, the systematic uncertainty from this is expected to be much smaller than the statistical precision of the dielectron \( v_2 \).

The systematic uncertainties of dielectron \( v_2 \) for the 2010 and 2011 data sets are studied separately and found to be comparable. For the combined results, the systematic uncertainties are taken as the average from the two data sets. Table IV lists sources and their contributions to the absolute systematic uncertainties for the dielectron \( v_2 \) values in different mass regions. For each mass region, the systematic uncertainties from the mixed-event unlike-sign and same-event like-sign background subtraction are negligible and not shown in Table IV.

FIG. 17. (Color online) The invariant yield and \( v_2 \) of electrons from heavy flavor decays [50] fitted with functions in minimum-bias Au + Au collisions at \( \sqrt{s_{NN}} = 200 \text{ GeV} \). The spectrum is fit with a function \( A[e^{B\sqrt{p_{T}^{2}+D(p_{T}^{2}+E)}+\sqrt{p_{T}^{2}+C/E}^2} \), where \( A, B, C, D, E, \) and \( F \) are fit parameters. The \( v_2 \) is fit with the same function as used to parametrize the meson \( v_2 \) shown in Fig. 15.

FIG. 18. The dielectron \( v_2 \) from the \( c \bar{c} \) contribution as a function of \( M_{\ell\ell} \) and \( p_{T} \) with a completely uncorrelated \( c \) and \( \bar{c} \).
uncertainties are $p_T$ dependent for each source. The total absolute systematic uncertainties are the quadratic sums of the different contributions.

### V. RESULTS

The measured dielectron $v_2$ as a function of $p_T$ for $M_{ee} < 0.14$ GeV/$c^2$ in different centralities from Au + Au collisions at $\sqrt{s_{NN}} = 200$ GeV are shown in Fig. 19. For comparison, the charged and neutral pion $v_2$ results [42,51] are also shown in Fig. 19. We parametrize the pion $v_2$ from low to high $p_T$, perform the Dalitz decay simulation, and obtain the expected dielectron $v_2$ from $\pi^0$ Dalitz decay shown by the dashed curve. The ratio of the measured dielectron $v_2$ to the expected is presented in Fig. 20. The simulated dielectron $v_2$ from $\pi^0$ Dalitz decay is consistent with our measurements in all centralities within 5–10%. We note that different nonflow effects in the dielectron $v_2$ analysis and the PHENIX $\pi$ $v_2$ analysis might contribute to differences between data and simulation.

Figure 21 shows the dielectron $v_2$ as a function of $p_T$ in minimum-bias Au + Au collisions at $\sqrt{s_{NN}} = 200$ GeV in six different mass regions: $\pi^0$, $\eta$, charm + $p^0$, $\omega$, $\phi$, and charm+thermal radiation, as defined in Table III. We find that the expected dielectron $v_2$ (dashed curve) from $\pi^0$, $\eta$, $\omega$, and $\phi$ decays is consistent with the measured dielectron $v_2$ for $M_{ee} < 1.1$ GeV/$c^2$. The dielectron $v_2$ in the $\phi$ mass region is consistent with the $\phi$ meson $v_2$ measured through the decay channel $\phi \rightarrow K^+K^−$ [44]. In addition, in the charm+thermal radiation mass region, dielectron $v_2$ can be described by a $c\bar{c}$ contribution within experimental uncertainties.

With the measured $p_T$-differential $v_2$ presented above and cocktail spectrum shapes detailed in Sec. III D, we obtain the dielectron integral $v_2$ for $|y_{ee}| < 1$, which is the yield weighted average for $p_T(e^+ e^-) > 0$. For the low $p_T$ region where the analysis is not applicable, we use the simulated differential $v_2$ for the extrapolation. The $p_T$ spectra of dielectrons might be different from those of cocktail components. For the mass region $0.2 < M_{ee} < 1.0$ GeV/$c^2$, we also use dielectron

### TABLE IV. Sources and their contributions to the absolute systematic uncertainties for dielectron $v_2$ measurements in different mass regions. The uncertainties for each source are $p_T$ dependent and listed as a range for each mass region. The total absolute systematic uncertainties are the quadratic sums of the different contributions. NR represents normalization range, bg represents background.

<table>
<thead>
<tr>
<th>Source/contribution</th>
<th>0–0.14</th>
<th>0.14–0.30</th>
<th>0.5–0.7</th>
<th>0.76–0.80</th>
<th>0.98–1.06</th>
<th>1.1–2.9 GeV/$c^2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>DCA cut</td>
<td>$(0.2–1.3) \times 10^{-3}$</td>
<td>$(0.6–2.8) \times 10^{-2}$</td>
<td>$(2.5–9.7) \times 10^{-2}$</td>
<td>$(0.4–3.7) \times 10^{-2}$</td>
<td>$(1.3–2.7) \times 10^{-2}$</td>
<td>$(0.9–12.5) \times 10^{-2}$</td>
</tr>
<tr>
<td>NR</td>
<td>$(0.2–1.3) \times 10^{-3}$</td>
<td>$(0.6–2.8) \times 10^{-2}$</td>
<td>$(2.5–9.7) \times 10^{-2}$</td>
<td>$(0.4–3.7) \times 10^{-2}$</td>
<td>$(1.3–2.7) \times 10^{-2}$</td>
<td>$(0.9–12.5) \times 10^{-2}$</td>
</tr>
<tr>
<td>bg method</td>
<td>$(0.1–0.4) \times 10^{-2}$</td>
<td>$(0.2–0.4) \times 10^{-2}$</td>
<td>$(0.1–0.6) \times 10^{-2}$</td>
<td>$(0.3–1.0) \times 10^{-2}$</td>
<td>$(0.3–2.8) \times 10^{-2}$</td>
<td>$(0.3–2.8) \times 10^{-2}$</td>
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<tr>
<td>$n\sigma$ cut</td>
<td>$(0.1–7.3) \times 10^{-3}$</td>
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<tr>
<td>$\eta$-gap</td>
<td>$(0.1–7.3) \times 10^{-3}$</td>
<td>$(0.1–7.3) \times 10^{-3}$</td>
<td>$(0.1–7.3) \times 10^{-3}$</td>
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<tr>
<td>Total</td>
<td>$(0.2–7.4) \times 10^{-3}$</td>
<td>$(0.6–2.8) \times 10^{-2}$</td>
<td>$(2.6–9.7) \times 10^{-2}$</td>
<td>$(0.5–3.7) \times 10^{-2}$</td>
<td>$(2.6–3.3) \times 10^{-2}$</td>
<td>$(4.9–13.0) \times 10^{-2}$</td>
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<tr>
<td></td>
<td></td>
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<td></td>
<td></td>
<td></td>
<td>$–(4.9–36.5) \times 10^{-2}$</td>
</tr>
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</table>
FIG. 20. (Color online) The ratio of the measured dielectron $v_2$ in the $\pi^0$ Dalitz decay region over the expected dielectron $v_2$ from $\pi^0$ Dalitz decay as a function of $p_T$ in different centralities from Au + Au collisions at $\sqrt{s_{NN}} = 200$ GeV. The dashed line is a constant fit to the ratio. The bars and bands represent statistical and systematic uncertainties, respectively.

$p_T$ spectra measured by PHENIX [10] and obtain the integral $v_2$ in these mass regions. The difference between this and the default case contributes additional systematic uncertainties for the integral $v_2$ measurements, which are smaller than those from other sources detailed in Sec. IV. Figure 22 shows the dielectron integral $v_2$ from data and simulation for $|y_{e^+e^-}| < 1$

FIG. 21. (Color online) (a)–(f) The dielectron $v_2$ as a function of $p_T$ in minimum-bias Au + Au collisions at $\sqrt{s_{NN}} = 200$ GeV for six different mass regions: $\pi^0$, $\eta$, charm + $\rho^0$, $\omega$, $\phi$, and charm + thermal radiation. Also shown are the neutral pion [42] $v_2$ and the $\phi$ meson $v_2$ [44] measured through the decay channel $\phi \rightarrow K^+ K^-$. The expected dielectron $v_2$ (dashed curves) from $\pi^0$, $\eta$, $\omega$, and $\phi$ decays in the relevant mass regions are shown in panels (a)–(e) while that from $c\bar{c}$ contributions is shown in panel (f). The bars and bands represent statistical and systematic uncertainties, respectively. The full difference between mixed-event unlike-sign and same-event like-sign background subtraction contributes to the lower bound of the systematic uncertainties, which leads to asymmetric systematic uncertainties in panel (f).
calculations for the velocities of hadrons, including charm quarks, in minimum-bias Au + Au collisions at √sNN = 200 GeV. Also shown are the corresponding dielectron v2 from hadronic matter and QGP thermal radiation and the sum of these two sources [54] are compared. The v2 for hadrons π, K, p, φ, and Λ are also shown for comparison. The bars and boxes represent statistical and systematic uncertainties, respectively. The systematic uncertainty for the first data point is smaller than the size of the marker.

For minimum-bias Au + Au collisions at √sNN = 200 GeV. Also shown are the corresponding dielectron v2 from hadronic matter and QGP thermal radiation and the sum of these two sources [54] are compared. The v2 for hadrons π, K, p, φ, and Λ are also shown for comparison. The bars and boxes represent statistical and systematic uncertainties, respectively. The systematic uncertainty for the first data point is smaller than the size of the marker.

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