Evaluation of Velocity Estimation Methods Based on their Effect on Haptic Device Performance

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Abstract—This paper comparatively evaluates the effect of real-time velocity estimation methods on passivity and fidelity of virtual walls implemented using haptic interfaces. Impedance width, or Z-width is a fundamental measure of performance in haptic devices. Limited accuracy of velocity estimates from position encoder data is an impediment in improving the Z-width in haptic interfaces. We study the efficacy of Levant’s differentiator as a velocity estimator, to allow passive implementation of higher stiffness virtual walls as compared to some of the commonly used velocity estimators in the field of haptics. We first experimentally demonstrate feasibility of Levant’s differentiator as a velocity estimator for haptics applications by comparing Z-width performance achieved with Levant’s differentiator and commonly used Finite Difference Method (FDM) cascaded with a lowpass filter. A novel Z-width plotting technique combining passivity and fidelity of haptic rendering is proposed, and used to compare the haptic device performance obtained with Levant’s differentiator, FDM+lowpass filter, First Order Adaptive Windowing and Kalman filter based velocity estimation methods. Simulations and experiments conducted on a custom single degree of freedom haptic device demonstrate that the stiffest virtual walls are rendered with velocity estimated using Levant’s differentiator, and highest wall rendering fidelity is achieved by First Order Adaptive Windowing based velocity estimation scheme.

I. INTRODUCTION

Impedance width, or Z-width is defined as the dynamic range of achievable impedances that can be rendered by a haptic interface device, where achievable impedances mean that impedances satisfy a robustness property, such as passivity [1]. The upper limit of Z-width is the maximum impedance that can be rendered by a haptic interface without any voluntary human motion induced instabilities [2]. Z-width is a fundamental measure of performance in haptic interfaces, and a higher Z-width means that a wide range of haptic environments can be rendered by the device. Z-width is an important metric to compare performance of haptic devices used for rendering complex virtual environments for surgical applications [3]. The haptic device must be able to render impedances that occur in such virtual environment interactions in a stable manner. Need for maximal Z-width performance has also been recognized as one of the essential requirements in haptic tele-manipulation of surgical robots [4]. Various strategies have been proposed to increase the Z-width of haptic interfaces, such as increasing the sampling frequency [5], increasing encoder resolution, adding physical damping [1], adding electrical damping [6], [7] and hybrid control algorithms that employ both active and passive actuators (such as magneto-rheological brakes) [8], [9]. Few researchers, however, have investigated the effect of velocity estimation accuracy on the Z-width performance. In one case, Hayward et al. proposed an Adaptive Windowing discrete-time velocity estimation technique and presented as an example its application to improve Z-width performance [10]. In other work, Gil explored the effect of FDM+filter parameters on the Z-width performance in simulation [11]. Colonnese and Okamura [12] presented explicit stability and quantization error regions for virtual spring and damper rendering, offered a software tool to identify system parameters necessary to satisfy desired haptic display objectives, and verified their findings experimentally. In [13], we proposed use of the Levant’s differentiator for estimating velocity, and presented preliminary results on Z-width improvement.

Finite Difference Method (FDM) is the most widespread method used for estimating velocity from position encoder data in haptic applications. As the sampling rates increase, the velocity resolution deteriorates significantly for FDM [14]. Cascading FDM with a lowpass filter is a common way of addressing the issue of poor velocity resolution at high sampling rates [1], but this comes at the cost of introducing a time-delay in velocity estimation. Time-delay in velocity estimation acts as another limiting factor in increasing the Z-width of haptic displays. There is a trade-off between the noise admitted and the time-delay in estimation: lower the cutoff frequency, less the noise admitted into the system, but with greater time-delay in estimations, and vice versa. This trade-off has been widely explored in the literature [15] and various velocity estimation schemes have been proposed to overcome the limitations of FDM+filter with varying degrees of success, such as adaptive windowing [16], time stamping [17], Kalman filter based [14], curve breaking velocity estimator [18] and Least Squares fit based [19] techniques. Tilli and Montanari discussed the shortcomings of FDM+filtering and other differentiation techniques, and proposed a switching filter approach for velocity estimations from discrete position readings in [20]. In [21], Koul et al. proposed a dual-rate sampling scheme that decouples the position and velocity control loops, and employs a slower sampling rate for velocity control loop to reduce the quantization effects in FDM based velocity estimation to improve the Z-width performance. Sinclair et al. [22] presented a comparative experimental evaluation of a variety of velocity estimation algorithms including several hybrid combinations of more than one algorithm.

Velocity estimation techniques from position encoder signal can be broadly divided into two categories: period counting and frequency counting methods. Period counting methods use specialized hardware to accurately measure the time elapsed between consecutive encoder ticks, and use that to estimate velocity [23], [24], [25]. A primary advantage of period counting methods is in very accurate estimation at low velocities, but the resolution degrades at higher velocities. Frequency counting methods use number of encoder ticks per unit time information to estimate the velocity. Zhu and Lamarche proposed a velocity estimation technique using both position and acceleration data, for damping enhancement in haptic devices [26]. Again, the drawback

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is the need for additional hardware. To circumvent differentiation induced effects, in [27] and [28] authors propose using fractional order control that employs differentiation and integration of arbitrary order. Controller designed using this approach is shown to enlarge the Z-width as compared to standard integer order differentiation based control. While this approach provides an additional degree of freedom in increasing Z-width, limitations exist due to sensitivity to changes in system parameters and distortion of effective inertia at higher frequencies. A good derivative estimation scheme should exhibit zero or minimum time-delay in estimations, provide increasing accuracy with increasing sampling frequency, robustness to fluctuations in input signal velocity, and offer ease of implementation on existing hardware. To that end, in our previous work [13], we proposed the use of the Levant’s differentiator for improved velocity estimations and increased Z-width in haptic interfaces.

Levant’s differentiator is a Second Order Sliding Mode (SOSM) control based real-time robust exact differentiation technique [29]. It is a nonlinear velocity observer which exhibits finite time convergence and increasing accuracy with increasing sampling rates. In [13] we performed a preliminary feasibility study of the Levant’s differentiator as a velocity estimator for haptic interfaces, and compared it with the FDM+filter method. Convergence of Levant’s differentiator is contingent upon the choice of several parameters, and a crude condition for choosing them was given by Levant in [29].

In this paper, we use the Lyapunov function analysis technique for SOSM systems proposed in [30] to extend the range of acceptable choice of parameters that would ensure convergence of Levant’s differentiator. Levant’s differentiator implementations with parameters chosen according to Levant’s recommendations, Lyapunov analysis and from experimental tuning are compared with FDM+lowpass filter method in their effectiveness in increasing Z-width performance of a custom one degree of freedom haptic device. We additionally propose a novel format for Z-width plots, which present virtual wall stiffness (K) vs. virtual wall damping (B). A detailed review of performance metrics for haptic interfaces by Samur in [2] presents the frequency domain max/min impedance range plotting method proposed by Weir et al. [7] as the state of art for quantifying the Z-width. However, frequency domain plots still do not provide information on accuracy of the rendered impedance. An improved plot was proposed by Baser et al. [8] where Z-Width is presented together with transparency bandwidth. In [31], Gil et al. presented a method of estimating Z-width using the experimental frequency response computed at different workspace positions, and critical stiffness values are then plotted as isolines in the workspace. This method extends the traditional Z-width plot by showing the dependence on workspace position, however does not inform about fidelity of the achievable impedances. Our plotting method simultaneously illustrates the stable K-B region and the fidelity of the rendering at each stable K-B pair, overcoming limitations with the traditional time-response based method of plotting Z-width that fails to capture the device inertia, mechanical resonances, and fidelity of the rendered virtual environment, and provides a more comprehensive fidelity measure. Our fidelity of rendering measure builds upon the frequency response based Z-width plotting method proposed in [7]. Colonnese et al. define the Average Distortion Error (ADE) as a metric for describing haptic accuracy and form an objective function to optimally

compute linear system model parameters in [32]. ADE quantifies frequency dependent difference between actual and desired dynamics, normalized by desired dynamics and multiplied by a weighting function. The fidelity measure employed in this paper can be thought of as a simplified ADE without normalization and a unity weighting function. This combined Z-width plot captures the practical limitations of haptic devices which are not evident in time-response based Z-width computation, and also provides information about fidelity of the commanded virtual environment. The idea is simple but effectively conveys the information about both stability and accuracy in an easily recognizable format. Our proposed Z-width plotting method is employed to compare the Levant’s differentiator with FDM+lowpass filter, First Order Adaptive Windowing (FOAW) and Kalman filter based methods in both simulations and experiments. Results show that among all the velocity estimation schemes considered, highest stiffness virtual walls are rendered with Levant’s differentiator, while First Order Adaptive Windowing enabled rendering virtual walls with highest fidelity.

II. REVIEW OF VELOCITY ESTIMATION METHODS

In this section we briefly review the velocity estimation methods considered in this paper. These methods are chosen based on their widespread use for estimating velocity in haptic applications.

A. FDM+lowpass filter

Finite Difference Method (FDM) is the most basic method of estimating velocity by computing the slope of two most recently sampled position data points, given as:

$$v_k = \frac{y_k - y_{k-1}}{T},$$

(1)

where $y_k$ is the discrete position signal obtained by sampling the continuous position signal $y(t)$ at $t = kT$ time instants, where $T$ is the sampling period. $v_k$ is the estimated velocity. However, high sampling rates ($\geq 1$ kHz) typically used in haptic applications will significantly amplify any noise present in $y_k$ [16]. The most commonly used method for removing high frequency noise in velocity estimations induced by FDM is implementing a low-pass filter. In our study, we used a second order Butterworth filter to remove the noise in FDM-based velocity estimations, which is a well-known and commonly used filter in haptic and other feedback control systems. The tunable parameter in FDM+filter method is the filter cutoff frequency $\omega_c$, which can be tuned to achieve best performance. We selected the filter cutoff frequency $\omega_c$ to maximize the Z-width performance as detailed in [15].

B. Kalman filter

Kalman filtering of the measured position signal based on a triple-integrator model to estimate velocity was proposed by Bélanger in [14]. Although a double-integrator model will suffice for estimating velocity, Bélanger recommends using a triple integrator model for increased accuracy. Using the notation in [16], a linear discrete stochastic model is used to represent the estimated state $x_k$ as:

$$x_{k+1} = Ax_k + Gw_k$$

and

$$y_k = Hx_k + e_k$$

(2) 

(3)
where \( \mathbf{x}_k = (x_k, x_k, x_k) \) is a vector of the estimated position \( x_k \) and its derivatives, \( A \) is the state transition matrix, \( H \) is the observation matrix and \( y_k \) is the position measured at \( k^{th} \) sampling instants. \( \mathbf{w}_k \) is the process noise and \( e_k \) is the measurement noise, both of which are assumed to be zero mean white Gaussian. Since we have assumed the triple-integrator model, \( A, G \) and \( H \) are given as:

\[
A = \begin{bmatrix} 1 & T & \frac{T^2}{2} \\ 0 & 1 & T \\ 0 & 0 & 1 \end{bmatrix}, \quad G = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}, \quad H = \begin{bmatrix} 1 & 0 & 0 \end{bmatrix}.
\] (4)

In the triple-integrator model, \( \mathbf{w}_k \) is viewed as a surrogate for derivative of acceleration, and therefore its covariance matrix \( Q_k \) can be written as

\[
Q_k(i, j) = \frac{q}{(3 - i)! (3 - j)! (7 - i - j)!} T^{7 - i - j}
\]

where \( q \) is a parameter that needs to be adjusted depending on the motion characteristics. We tuned the parameter \( q \) in simulation to maximize the impedance width performance. Typically, in commercially available haptic devices, position is sensed from an optical position encoder, where error in measurement is predominantly due to quantization, such that \(-d \leq e_k \leq d\) where \( d \) is the encoder resolution. Thus, variance for the measurement error \( e_k \) is given as \( r = \text{var}(e_k) = d^2/3 \). Based on the above model, an Adaptive fading Kalman Filter can be written to estimate velocity as detailed in [16] and [33].

C. Adaptive windowing

Janabi-Sharifi et al. proposed a discrete-time First Order Adaptive Windowing (FOAW) method which addresses the noise amplification issue present in FDM by adaptively changing the window size for computing the velocity based on the signal itself [16]. This is equivalent to adaptively changing the sampling rate. Window size is chosen short when the velocity is high, and large when velocity is low; thereby providing more precise and reliable velocity estimates. The goal is to find a straight line that passes through the sampled data \( y_k, y_{k-n} \) over a window of length \( n \) where \( n = \max\{1, 2, 3, \ldots\} \) such that

\[
|y_k - y_{k-i}| \leq d, \quad \forall i \in \{1, 2, 3, \ldots, n\}
\] (5)

where \( y_{k-i} = a_n + b_n (k - i) T \). For Best-fit-FOAW solution, the coefficients \( a_n \) and \( b_n \) are given as:

\[
a_n = \frac{k y_k - \sum_{i=0}^{n} (n - k) y_{k-i}}{n} \quad \text{and} \quad b_n = \frac{n \sum_{i=0}^{n} y_{k-i} - 2 \sum_{i=0}^{n} i y_{k-i}}{n (n + 1) (n + 2) / 6}.
\] (6)

Here \( b_n \) is the slope of the best-fit line computed using least-squares approximation which minimizes the error energy. The estimated velocity is \( \dot{y}_k = b_n \). The algorithm for FOAW is given in [16].

III. LEVANT’S DIFFERENTIATOR FOR VELOCITY ESTIMATION

Levant proposed a robust exact differentiation technique using SOSM for signals with a given upper bound on the Lipschitz’s constant of the derivative [29]. Given an input signal \( f(t) \), the Lipschitz’s constant of the derivative is a constant \( C \) which satisfies

\[
|\dot{f}(t) - \dot{f}(t_2)| \leq C |t_1 - t_2|
\] (7)

If the second derivative of the base signal exists, then the Lipschitz’s constant in (7) satisfies

\[
\sup_{t \geq 0} \left| \frac{d^2}{dt^2} f(t) \right| \leq C
\] (8)

Consider \( x(t) \) an estimate of the input signal \( f(t) \). Define error in the estimate as \( e(t) = x(t) - f(t) \), then the first order derivative can be estimated as

\[
\dot{x}(t) = u(t), \quad u(t) = u_1(t) - \lambda |e(t)|^{1/2} \text{sign}(e(t))
\]

\[\dot{u}_1(t) = -\alpha \text{sign}(e(t)) \] (9)

The solution of the system described by equation (9) is under-

\[
V(x) = 2\alpha |x_1| + \frac{1}{2} |x_2|^2 + \frac{1}{2} \lambda |x_1|^{1/2} \text{sign}(x_1) - x_2 \]

\[= \zeta^T P \zeta \] (13)

where \( \zeta = [|x_1|^{1/2} \text{sign}(x_1), x_2]^T \) and

\[P = \frac{1}{2} \left[ \begin{array}{cc} 4\alpha + \lambda^2 & -\lambda \\ -\lambda & 2 \end{array} \right] \]

Using the Lyapunov function candidate detailed above and following the analysis detailed in [30], the stability conditions

\[
\alpha > C, \quad \lambda^2 \geq 4C \frac{\alpha + C}{\alpha - C}
\] (10)

An easier choice of the parameters given in the same reference is

\[
\alpha = 1.1 C, \quad \lambda = C^{1/2}
\] (11)

It should be noted that conditions (10) and (11) result from a very crude estimation of the convergence criterion.
derived from the Lyapunov Function Based Approach (LFBA) are given as:

$$\alpha > 3C + \frac{2C^2}{\lambda^2}; \lambda > 0 \quad (14)$$

The stability conditions obtained from the HBA and LFBA can be compared by using the parameterization $\alpha = \mu_1 C$ and $\lambda = \mu_2 C^{1/2}$, to eliminate the Lipschitz’s constant $C$ from the inequalities. The plots of $\mu_1$ vs. $\mu_2$ give the parameterized stable regions as shown in Fig. 1. It can be observed that LFBA stability conditions, while not wholly encompassing the HBA conditions, do extend the range of choice for the parameters $\alpha$ and $\lambda$. It is observed that the HBA-Special Case (HBA-SC) gain pair given by (11) lies outside of the both regions. Since both LFBA and HBA give only sufficient conditions, it is possible to choose a gain pair which lies outside these stability ranges but still ensures convergence. For this study, the gains were chosen to satisfy the stability conditions and maximize Z-width performance in simulation.

IV. FEASIBILITY OF LEVANT’S DIFFERENTIATOR FOR INCREASING Z-WIDTH

In this section, we investigate the feasibility of Levant’s differentiator as a velocity estimator in increasing the Z-width performance in haptic interfaces. We followed the automated Z-width estimation experimental protocol described in [13] to estimate the Z-width of a custom linear impedance type haptic device shown in Fig. 2. Control of the haptic device was implemented in Simulink® and QuaRC® on a host computer running Windows®. The code is compiled and downloaded on a target computer running QNX® RTOS, which is interfaced to the haptic device through a Q4 DAQ from Quanser Inc. The sampling rate was set at 10 kHz.

A spring-damper virtual wall was implemented and Z-width was computed using time-response data collected during virtual wall hit trials. The virtual wall stiffness ($K$) and virtual wall damping ($B$) values were varied and the pairs of $(K, B)$ which presented a marginally passive virtual wall interaction are recorded. For evaluating the feasibility of Levant’s differentiator, the Z-width plot is computed for the following velocity estimation methods:

1) Levant’s differentiator with the HBA-SC gains.
2) Levant’s differentiator with the LFBA gains.
3) Levant’s differentiator with experimentally adjusted gains.
4) FDM cascaded with a second order Butterworth filter with 1000 Hz cutoff frequency.

The value of Lipschitz’s constant is calculated by collecting the position data during a virtual wall hit with velocity estimated using FDM cascaded with a second order Butterworth filter, and calculating the analytical double derivative of a sum of sines function fitted to the position data. The cutoff frequency for the Butterworth filter was chosen experimentally to get the maximum Z-width performance.

It is observed in Fig. 3 that use of Levant’s differentiator with adjusted gains for velocity estimation extends the Z-width of the device (higher virtual wall stiffness), as compared to using FDM+filter for the same purpose. Levant’s differentiator with HBA and LFBA based gains performs better than FDM+filter for damping values up to 150 Ns/m, but is found to be conservative.
selected for the nominal case by estimating $\lambda$ for Levant’s differentiator with adjusted gains. The reason for this sharp drop is that $K$ and $B$ increase, the gains $\alpha$ and $\lambda$ increase. The haptic device impedance is estimated by providing an external multi-sine excitation signal $(K, B)$ pair in an exhaustive grid-search. The search terminates when $K \rightarrow 0$. Fig. 5 shows the graphically. Fidelity of the rendered virtual wall is quantified by computing the Root Mean Square (RMS) difference between the magnitude plots of the estimated impedance transfer function and the ideal spring-damper transfer function as shown in Fig. 6. This RMS difference is a measure of how well the rendered wall matches the commanded spring-damper virtual wall. Conventional methods of plotting Z-width only show the range of impedances that satisfy the passivity condition (i.e. phase is between $\pm 90$ degrees), however this added metric captures the fidelity of a desired impedance when rendered by a haptic interface. Quantifying performance of a haptic interface in rendering a given impedance should involve assessing both the passivity and fidelity of rendered impedance. It can be observed that at low frequencies the magnitude plot of estimated impedance matches the ideal wall impedance quite well, but at higher frequencies the device inertia becomes prominent and the controller can no longer render the commanded virtual wall. The slight attenuation in magnitude of the estimated impedance at low frequencies can be attributed to nonlinearities such as friction, quantization and sampling.

The velocity estimation methods described in Section II are compared in simulations and experiments using our proposed Z-width plotting method. For simulation, the device model parameters were identified by performing frequency domain system identification of the haptic device shown in Fig. 2 using a Schröeder phased input signal [35] and the System Identification Toolbox© in Matlab©. Static and kinetic friction are assumed to be the same, and was estimated a priori and compensated before performing frequency domain system identification. A mass-damper model with Coulomb friction was assumed, and the estimated parameters were mass $m = 0.52$ kg, damping $b = 13.2$ Ns/m and Coulomb friction $f_c = 0.19$ N. The haptic device
Fig. 6. Estimated impedance of the haptic device compared with the ideal impedance expected from a spring-damper virtual wall. Note that at higher frequencies, device inertia becomes prominent and the deviation from ideal spring-damper virtual wall case increases.

Table I compares the experimental Z-width results for various differentiation schemes along following metrics: maximum rendered stiffness (K-width), maximum rendered damping (B-width), maximum fidelity error and number of parameters to be tuned. These metrics are chosen to compare the suitability of differentiation schemes for any given application. It can be seen that Levant’s differentiator is able to achieve highest K-width, but is limited in B-width. Furthermore, Levant’s differentiator requires two parameters to be tuned and displays second highest fidelity error. Both FDM+filter and AKF display intermediate K-widths and require a single parameter to be tuned. FDM+filter is able to achieve highest B-width, but also has highest fidelity error of all schemes. FOAW displays smallest K-width, but requires no parameter tuning and displays smallest fidelity error. None of the schemes perform best across all the metrics, so depending on the application, appropriate scheme (or combination thereof) needs to be selected. For example, if low damping and high stiffness is desired, then Levant’s differentiator is a good choice, but if intermediate damping and stiffness are desired, then FOAW is better. A combination of multiple differentiation schemes, such as FOAW and Levant’s differentiator could potentially result in better performance than each of them individually.

In related work, Sinclair et al. [22] experimentally compared a variety of velocity estimation algorithms. They optimized each algorithm’s relevant parameters using a pure adaptive search method to minimize a multi-objective criterion that took into account both the delay and the error in delay-corrected velocity estimations. Based on this criterion, third order Kalman estimators that were hybrid combinations of the Kalman estimator with Levant’s differentiator or FOAW produced the smallest error in estimations. The focus of the work was realistic haptic simulation of stick-slip sensations, therefore virtual-wall specific evaluations of the estimators were outside the scope of this work. Indeed, Sinclair et al. pointed to the distinctly different aspects of performance that virtual wall and stick-slip haptic simulations require from velocity estimators. The FOAW method did not perform well in comparison with the other algorithms in Sinclair et al.’s work. In our work, however, it has shown the best performance when viewed from the haptic fidelity perspective.

In this paper, we have only considered the SOSM based robust exact differentiation technique proposed by Levant in [29]. Other variations and extensions to this technique have been proposed since then combine the SOSM and Linear observers and/or propose variable gain structure where the parameters $\alpha$ and $\lambda$ are updated according to a set of relations [36], [37], [38]. These extensions introduce more parameters which need to be selected and tuned based on simulation or experiments, thus increasing the complexity of the implementation. When properly tuned, these extensions to SOSM based velocity observer may provide better velocity estimates than the standard Levant’s differentiator discussed in this paper.

Successful implementation of Levant’s differentiator for velocity estimation demonstrated increased K-width performance in haptic interfaces as compared to FDM+filter, AKF and FOAW velocity estimation methods in both simulations and experiments. Ease of implementation and finite-time convergence characteristics of the Levant’s differentiator makes it an attractive option for use as a velocity estimator in haptics and other feedback control system applications.
Fig. 7. Z-width plots obtained in simulation for various velocity estimation methods. The colorbar shows the RMS error (in Ns/m) between estimated and ideal virtual wall impedance. It is observed that highest virtual wall stiffness is obtained with Levant’s differentiator, then AKF, followed by FDM+filter and FOAW. The fidelity of haptic rendering deteriorates at higher virtual wall stiffness values for all velocity estimation methods.

TABLE I

<table>
<thead>
<tr>
<th>Differentiation Scheme</th>
<th>K-width (N/m)</th>
<th>B-width (Ns/m)</th>
<th>Tunable parameters</th>
<th>Max. fidelity error (Ns/m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>FDM+filter</td>
<td>$2.4 \times 10^5$</td>
<td>160</td>
<td>$\omega_c$</td>
<td>894.91</td>
</tr>
<tr>
<td>FOAW</td>
<td>$2.1 \times 10^4$</td>
<td>120</td>
<td>None</td>
<td>294.3</td>
</tr>
<tr>
<td>AKF</td>
<td>$2.7 \times 10^4$</td>
<td>100</td>
<td>$q$</td>
<td>520.04</td>
</tr>
<tr>
<td>Levant’s differentiator</td>
<td>$3.6 \times 10^4$</td>
<td>100</td>
<td>$\alpha, \lambda$</td>
<td>614.19</td>
</tr>
</tbody>
</table>

VI. CONCLUSION

In this paper, we investigated the feasibility of Levant’s differentiator for estimating velocity from position encoder data to increase the Z-width performance of haptic devices, and compared it with Finite difference method + lowpass filter, Kalman filter and First Order Adaptive Windowing velocity estimation schemes. We proposed a novel method for plotting Z-width, which combines the information about fidelity of the rendered haptic environment and practical device characteristics based on the frequency-response with the intuitive appeal of traditional Z-width obtained with the time-response of the haptic device. The proposed Z-width plotting method addresses the shortcomings of time-response based Z-width plot by capturing the practical device limitations and also adding another dimension that informs about the accuracy of rendered virtual wall. Velocity estimation methods were evaluated using our proposed Z-width plotting scheme. Simulation and experimental results demonstrate that highest stiffness virtual walls were rendered using Levant’s differentiator for velocity estimation, and FOAW was able to render virtual walls with highest fidelity. Insights gained through this study can be directly applied to surgical simulators that necessarily render complex virtual environments with high fidelity, and to haptic tele-manipulation of surgical robots that must faithfully and stably transmit a wide range of impedances.
Fig. 8. Z-width plots obtained experimentally for various velocity estimation methods. The colorbar shows the RMS error (in Ns/m) between estimated and ideal virtual wall impedance. Similar observations as those in Fig. 7 can be made here.

ACKNOWLEDGMENT

This work was supported in part by the NSF Grant CNS-1136099.

REFERENCES


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