Reduced electronic correlation effects in half substituted $\text{Ba}(\text{Fe}_{1-x}\text{Co}_x)_2\text{As}_2$

Z.-H. Liu,^{1,2,a)} A. N. Yaresko,³ Y. Li,⁴ D. V. Evtushinsky,¹ P.-C. Dai,⁴ and S. V. Borisenko^{1,b)}

¹Institute for Solid State Research, IFW Dresden, D-01171 Dresden, Germany

²State Key Laboratory of Functional Materials for Informatics, SIMIT, Chinese Academy of Sciences, Shanghai 200050, China

³Max Planck Institute for Solid State Research, D-70569 Stuttgart, Germany

⁴Department of Physics and Astronomy, Rice University, Houston, Texas 77005-1827, USA

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We report a comprehensive study of the tridimensional nature and orbital character of the low-energy electronic structure in 50% Cobalt doped $\text{Ba}(\text{Fe}_{1-x}\text{Co}_x)_2\text{As}_2$ ($d^{6.5}$), by using polarization- and photon energy-dependent angle-resolved photoemission spectroscopy. An extra electron-like Fermi surface is observed around the Brillouin zone boundary compared with isoelectronic $\text{K}_y\text{Fe}_{2-x}\text{Se}_2$ ($d^{6.5}$). The bands near the Fermi level (E_F) are mainly derived from Fe/Co $3d\ t_{2g}$ orbitals, revealing visible dispersions along the k_z direction. In combination with the local density approximation and the dynamical mean-field theory calculations, we find that the As $4p$ bands are non-renormalized and the whole $3d$ band needs to be renormalized by a “single” factor of ~ 1.6 , indicating moderate electronic correlation effects. The “single” factor description of the correlation strength among the different $3d$ orbitals is also in sharp contrast to orbital-dependent correlation effects in BaFe_2As_2 . Our findings indicate a remarkable reduction of correlation effects with little difference among $3d$ orbitals in BaFeCoAs_2 , due to the increased filling of the electronic $3d$ shell in the presence of significant Hund’s coupling. The results support that the electronic correlation effects and multiple orbital physics play an important role in the superconductivity of the 122 system and in other ferropnictides. *Published by AIP Publishing.* <https://doi.org/10.1063/1.5034488>

By application of either high pressure or chemical substitution, the superconductivity can be induced in ferropnictide,^{1,2} which is a family of superconducting compounds with critical temperatures (T_c) being the second highest to those of the cuprates. In the case of cuprates, the Mott insulating ground state of the parent non-superconducting materials inspired theorists to describe high temperature superconductivity originating from a strongly correlated matter. Heated debates for electronic correlation of iron-based superconductors (IBSs) have been going on.^{3–5} On the one hand, the low-energy electronic band structure is well described by the mean field theory calculation,⁶ which suggests the property of itinerant electrons. On the other hand, the bandwidth renormalization is needed to capture the essential dispersive features according to the results of the dynamical mean-field theory (DMFT)^{7,8} or the angle-resolved photoemission spectroscopy (ARPES),^{9–15} which indicates non-negligible electronic correlations in IBS.

The band structure of the 122 system is extensively studied by theoretical and experimental methods since doping of both electrons [$\text{Ba}(\text{Fe}_{1-x}\text{Co}_x)_2\text{As}_2$] and holes ($\text{Ba}_{1-x}\text{K}_x\text{Fe}_2\text{As}_2$) can suppress magnetic order and lead to a dome of superconductivity before reaching a more conventional metal or Mott insulator. The dopant not only introduces extra carriers and shifts the chemical potential up or down but also further tunes $3d$ shell away from or close to the half filling, which signifies a Mott insulator in strong correlation theory owing to the strong coulomb interaction. A study of hole over-doped BaFe_2As_2 evidenced an unusual non-Fermi-liquid behavior with frozen

moments in the paramagnetic phase, indicating the strong band renormalization near the Fermi level (E_F).⁸ Along with the increased filling of the electronic $3d$ shell and the decreased strength of electronic correlation, the crossover is found toward a Hund’s metal state, for which the correlation is more sensitive to J than to U .^{16–19} Additionally, one finds that a single global renormalization factor does not suit each band.^{13–15} Hund’s rule coupling dominates the orbital-dependent correlation strength in the expected regime, where the t_{2g} orbitals are more correlated than e_g ones; in particular, the d_{xy} orbital is the most correlated of all.^{5,20} These results exhibit that electronic correlation and the multi-orbital physics play an important role in the system.

In this work, we present ARPES results on 50% Cobalt doped $\text{Ba}(\text{Fe}_{1-x}\text{Co}_x)_2\text{As}_2$ using different polarized photons in a wide energy range. The number of $3d$ electrons of BaFeCoAs_2 ($d^{6.5}$) is at the middle of BaFe_2As_2 (d^6) and BaCo_2As_2 (d^7). We observed one electron-like Fermi surface (FS) at the Brillouin zone (BZ) center, one electron-like FS near the zone boundary, and two large electron-like FSs at the zone corner. They mainly originate from the Fe/Co $3d\ t_{2g}$ orbitals with evident k_z dispersions. The chemical potential shifts up about 0.24 eV compared with the parental BaFe_2As_2 .^{11,21–23} In combination with the local density approximation (LDA) and the DMFT calculations, we find that an overall band renormalization of about 1.6 is needed to capture the essential dispersive features, indicating much weaker correlation effects than in BaFe_2As_2 and a relatively strong correlation effect than in BaCo_2As_2 , for which the renormalization factors of 3 and 1.4 were reported, respectively.^{11,24} Unlike in the regime of hole-doped and electronic under-doped BaFe_2As_2 ,^{13–15} the electronic correlation strengths are little different among $3d$

^{a)}Email: liuzhonghao17@163.com

^{b)}Email: s.borisenko@ifw-dresden.de

FIG. 1. (a) Integrated intensity plot at E_F (± 10 meV) of BaFeCoAs₂ in σ geometry using $h\nu = 80$ eV at $T = 1$ K. (b) Intensity plots of band dispersion along $X\Gamma X$ and MXM directions, as indicated in (a). Dashed lines are guides to the eye for the band dispersions. (c) Sketch of the experimental polarization setup. The σ and π polarizations are for electric fields perpendicular and parallel to the mirror plane (red), respectively. (d) Calculated FSs at ΓXM and ZRA planes using the LDA calculation. The calculation details will be stated in the content later. (e) LDA bands along the high symmetry lines in the first BZ.

orbitals in BaFeCoAs₂. Combined with previous studies, our findings support that Hund's rule coupling plays the crucial role in ferropnictide materials.^{16,17,20,25,26} The strength of electronic correlations is efficiently tuned by changing the filling of the electronic 3d shell.

High quality single crystals of BaFeCoAs₂ ($T_c = 0$) were synthesized by the flux method. Samples with the size smaller than 1×1 mm² were cleaved *in situ*, yielding a flat mirror like (001) surface. ARPES measurements were performed using synchrotron radiation, 1-cubed ARPES end station at BESSY, within a wide range of photon energies and various polarizations. The optimum energy and momentum resolutions were ~ 10 meV and ~ 0.02 Å⁻¹, respectively, for the low temperature measurements. During measurements, the pressure was maintained better than 5×10^{-11} Torr. From our experimental setup shown in Fig. 1(c), we can observe that the high-symmetry directions and the normal of the sample surface define a mirror plane. The π (σ) geometry refers to the electric fields of the incident photons within (normal to) the mirror plane, respectively. The even (odd) orbitals with respect to the mirror plane are detected in π (σ) geometry. Here, we note that our experimental setup for the σ geometry includes a polarization component along z .

Figure 1(a) shows the measured FS map of BaFeCoAs₂ at 1 K using 80 eV in σ geometry. To identify which FSs are represented by intensity spots on the map, we have recorded the energy-momentum distributions of the photocurrents along the $X\Gamma X$ (RZR) and MXM (ARA) direction, as shown in Fig. 1(b). There are four electron-like bands near E_F , i.e., one at the zone center, one near the zone boundary, and two centered around the zone corner, named κ , ε , γ , and σ , respectively. In comparison with typical FS topology in IBS,⁹⁻¹⁴ an additional electron-like FS turns up at the zone boundary, which is consistent with calculated FS, as shown in Fig. 1(d). The measured FS at 80 eV is rather similar to the calculated FS at the ΓXM plane, indicating that the photon energy of 80 eV closely corresponds to the Γ plane along the k_z direction. Comparing the FSs at the ΓXM plane and the ZRA plane in Fig. 1(d), it can be observed that all of FSs show visible k_z dispersion, revealing the 3-dimensional (3D) nature of FSs in BaFeCoAs₂. Figure 1(e) shows the LDA calculated bands along the high symmetry lines in the BZ. Indeed, the low-energy electron dynamics in the 122 system is defined by

3d electrons and the only principal difference is that the half of these 3d electrons in the case of BaFeCoAs₂ stems from Co atoms. Apparently, this is not a significant variation from the point of view of the LDA theory.^{8,9}

To investigate the k_z dispersion, we carried out measurements in π geometry using photon energies ($h\nu$) from 28 to 90 eV, which covers more than 1.5 BZs along k_z . Figure 2(a) shows the intensity at E_F as a function of photon energy and $k_{||}$ oriented along the ΓX (ZR) direction. This plot implies that the κ band has a strong k_z dispersion, with a band minimum at Γ ($\sim 48, 76$ eV) and a band maximum at Z ($\sim 36, 62$ eV). The k_z variation of the κ band is also well illustrated by the intensity plots along the ΓM and ZA lines, as shown in Figs. 2(b) and 2(c), respectively. Comparing the top of the α band at the Γ point and Z point, one finds an appreciable k_z variation of α with an opposite tendency of that in κ .

Figures 2(c) and 2(d) show the intensity plots of band dispersion along ZA in π and σ geometries, respectively. The data taken with different geometries allow us to detect the orbital character of the bands. According to the symmetry analysis and by analogy with others IBS,^{12-15,27-31} we identify the orbital character of each band. At the Z point,

FIG. 2. (a) Intensity plot in the $h\nu$ - $k_{||}$ plane of BaFeCoAs₂ in π geometry (± 10 meV integration centered at E_F). (b) Intensity plot of band dispersion along ΓM (48 eV) in π geometry. (c) and (d) Intensity plots of band dispersion along ZA (62 eV) in π and σ geometries, respectively. The dashed lines are guides to the eye.

the α and κ bands are enhanced only in π geometry. They should be of d_{xz} character. The α' and β bands are highlighted only in σ geometry, and they have d_{yz} and d_{xy} orbital character. At the A point, the δ band can be seen in both geometries and the γ band is only detected in σ geometry, suggesting that δ is of d_{xz} and d_{yz} and γ is of d_{xy} orbital character.

After study of the FSs and the band structure with their orbital character by ARPES, we investigated the electronic correlation by comparing the energy bandwidths between experiments and calculations. We performed calculations based on the LDA + DMFT for BaFeCoAs₂ with the experimental crystal structural parameters $a = 3.955 \text{ \AA}$ and $c = 12.813 \text{ \AA}$. The internal coordinate, $z_{\text{As}} = 0.35405$, was relaxed by energy minimization for the ordered cell. The interaction parameters were chosen as $u = 5.0 \text{ eV}$ and $J = 0.9 \text{ eV}$. The LDA results were obtained using the PY LMTO computer code.³² The DMFT was performed with WIEN2K and the ALPS CTQMC hybridization solver with full charge-selfconsistency.

Figure 3 shows the experimental band dispersions along the high symmetry directions in π and σ geometries, respectively. LDA calculated bands were appended with red (3d bands) and black (4p bands) curves. The 3d bands near E_F calculated by LDA need to be narrowed 1.6 times to fit the experimental data and the 4p bands at high bind energy do not need any narrowing. The unnormalized 4p bands are also found in NaFeAs and FeSe compounds.^{33,34} To much accurately survey the renormalization factor of the 3d bands, we presented the second derivative intensity plot along ZRA lines in π and σ geometries appending renormalized LDA bands by a factor of 1.6, as shown in Fig. 4(a). The data taken in $k_z = \pi$ plane with two different geometries allow us to detect all 3d bands near E_F . The ω band with d_{z^2} character is enhanced by the z component in the σ geometry. Indeed, a “single” renormalization factor of 1.6 is only needed to capture the essential dispersive features. Besides, we also employed the DMFT to study the factor of the 3d bands with different orbital characters. The DMFT results appended with 1.6 times narrowed density functional theory (DFT) calculation bands are shown in Fig. 4(b). The orbital dependence renormalization factors in DMFT are 1.588, 1.564, 1.651, and 1.591 for xz/yz , xy , $x^2 - y^2$, and z^2 , respectively. Apparently, the numbers change just a little bit. Although the FS topology is no change upon the introduction of correlations, there is a significant mismatch of the bands right above E_F at the Γ point [marked by the red circle in Fig.

FIG. 3. The experimental band dispersions along the high symmetry directions of BaFeCoAs₂ in π and σ geometries, respectively. LDA calculated bands were appended with red (3d bands) and black (4p bands) curves. The 3d bands calculated by LDA are narrowed 1.6 times to fit the experimental data and the 4p bands are not narrowed.

FIG. 4. (a) Second derivative intensity plot along ZRA lines of BaFeCoAs₂ in π and σ geometries, appending renormalized LDA bands by a factor of 1.6. The orbital characters and polarizations are indicated. (b) LDA + DMFT calculations along the high symmetry lines. The bright color lines are calculated by the LDA + DMFT, and the black lines correspond to the DFT calculated bands renormalized by a factor of 1.6.

4(b)], which can be explained in terms of correlation effects and the evidence of inter-band coupling. The downshift band can account for the shadow near E_F at the Γ point, as shown in Figs. 1(a), 2(a), and 2(b).

As demonstrated above, the calculated 3d bands need to be renormalized by a “single” factor of ~ 1.6 to well duplicate the experimental data. Our finding suggests that the electronic correlation effects in BaFeCoAs₂ ($d^{6.5}$) are much weaker than in parental BaFe₂As₂ (d^6) and little stronger than in fully electron doped BaCo₂As₂ (d^7), for which the renormalization factors of 3 and 1.4 were reported.^{11,24} Additional, the correlation strengths were little different among orbitals, unlike in the regime of electron underdoped and hole-doped BaFe₂As₂, where the d_{xy} orbital is obviously prominent.^{13–15} The overall view of the 122 system and the electronic correlation strengths are tuned by the filling of electrons in the 3d shell. In the superconducting region, it is dominated by Hund’s rule coupling, which in turn decouples the charge excitations in different orbitals, so that the system reveals orbital-dependent electronic correlation effects.⁵ Along with more electrons filling the 3d shell, the system comes into moderately correlated Fermi liquid, as in BaFeCoAs₂. In this process, the electronic correlation strength of the t_{2g} orbital, d_{xy} in particular, evidently reduces and follows the global tendency. In consideration of the correlation effects helping to get high- T_c superconductors, the hole doped Ba_{1-x}K_xFe₂As₂ should hold a much larger superconducting region and higher T_c than electron doped Ba(Fe_{1-x}Co_x)₂As₂.

In addition, 1.6 times narrowing of the low-energy dispersions on BaFeCoAs₂ is also less than in an isoelectronic

$\text{K}_y\text{Fe}_{2-x}\text{Se}_2$ ($d^{6.5}$), for which 2.5 times narrowing was reported.¹¹ In $\text{K}_y\text{Fe}_{2-x}\text{Se}_2$, local antiferromagnetic exchange interaction was proposed as a serious candidate for the pairing mechanism.³⁵ We consider two differences of the two materials to explain that why $\text{K}_y\text{Fe}_{2-x}\text{Se}_2$ is a superconductor and the isoelectronic BaFeCoAs_2 is not. From the view of the real space, the antiferromagnetic exchange between Fe-Fe atoms can be destroyed by the heavy Co doping. While in the respect of the momentum space, the additional electron-like FS at the zone boundary increases the density of states near E_F and causes the itinerant behavior of the $3d$ electrons. In electron fully doped BaCo_2As_2 , the electronic correlation is much less important than in the ferropnictide.²³ The itinerant electron behavior is suggested in BaCo_2As_2 by observation of ferromagnetic characters in resistivity measurements³⁶ and nuclear magnetic resonance (NMR) experiments.³⁷

In summary, we study the FSs and the low-energy band structure on BaFeCoAs_2 by using the ARPES and the LDA + DMFT calculations. The system shows moderately correlated Fermi liquid behavior. Combined with previous studies, our findings indicate strong doping- and orbital-dependent correlation effects in 122 compounds.

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